Chapter 2. Systems of Linear Equations

### 2.1 Introduction;

consistent, backward substitution, forward substitution
2.2 Direct Methods for solving linear systems;

Gaussian elimination method, REF, RREF
2.3 Spanning sets and Linear Independence

Definitions, determine spans, linearly independence

### 2.4 Applications

Network problem, electrical circuit problem

## Chapter 3. Matrices

3.1 Matrix operations

Addition, subtraction, scalar multiplication, matrix multiplication, Applications
3.2 Matrix Algebra

Properties, transpose, symmetric matrices

### 3.3 The inverse of a matrix

Def, Inverse of 2 by 2 matrix, transpose and inverse, elementary matrices, Factorization of matrix into elementary matrices, inverse matrix of 3 by 3 matrix

Fundamental theorem of invertible matrices; version I

### 3.4 LU factorization

How to factor $A$ into $L U$, solving a system using LU factorization
3.5 Subspaces, Basis, Dimension, and Rank

Definitions of all these, subspaces associated with matrices, The rank theorem
Fundamental theorem of invertible matrices; version II

### 3.6 Linear transformation

Definition, standard matrix representation, homogeneous coordinate system, two linear transformations applied

### 3.7 Applications

Graph theory, adjacency matrix

Chapter 4. Eigenvalues and eigenvectors

### 4.1 Introduction

Definitions, Check eigenvalue and eigenvector, geometric meaning

### 4.2 Determinants

Definition, Laplace expansion theorem for determinants, Properties of determinants, Cramer's Rule, Cofactor method for inverse matrix
4.3 Eigenvalues and eigenvectors for n by n matrices

Characteristic polynomial, some properties of eigenvalues and eigenvectors
Fundamental theorem of invertible matrices; version III, higher power of matrix

### 4.4 Similarity and Diagonalization

Definition, theorem 4.22, diagonalizable or not, high power of a diagonalizable matrix
4.5 \& 4.6 Application: Markov Chain, solving a system of first order DE

Chapter 5. Orthogonality

### 5.1 Orthogonality in $\mathbb{R}^{n}$

Orthogonal set, Orthogonal basis, linear combination in terms of orthogonal (orthonormal) basis, Orthogonal matrix, Properties of orthogonal matrix,
5.2 Orthogonal Complements and orthogonal projections

Definition, four fundamental subspaces associated with a matrix, orthogonal projections

### 5.3 Gram Schmidt Process and the QR factorization

Gram Schmidt process, QR factorization, solving a system using QR factorization

### 7.3 Least Squares Approximation (Application of Orthogonal Projection)

Find the least squares solution of a linear system, application problem

## Study tip to prepare well for the final exam

1. Review your past hour exams carefully.
2. Review all problems in review for final thoroughly.
3. Make a sample final and try it!
4. Remember that your final exam score can change your final grade significantly.
( positively or negatively )

Final exam: Wednesday, Dec 11, 1:30-3:30 pm

