

## Chapter 6



- This Slideshow was developed to accompany the textbook
  - *Big Ideas Algebra 2*
  - *By Larson, R., Boswell*
  - *2022 K12 (National Geographic/Cengage)*
- Some examples and diagrams are taken from the textbook.

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## 6-01 Exponent Properties and $e$ (5.2, 6.2)

After this lesson...

- I can simplify expressions with exponents.
- I can simplify expressions involving  $e$ .
- I can rewrite expressions with  $e$  as decimals.

## 6-01 Exponent Properties and e (5.2, 6.2)

### • Using Properties of Rational Exponents

- $x^m \cdot x^n = x^{m+n}$  (Product Property)
- $(xy)^m = x^m y^m$  (Power of a Product Property)
- $(x^m)^n = x^{mn}$  (Power of a Power Property)
- $\frac{x^m}{x^n} = x^{m-n}$  (Quotient Property)
- $\left(\frac{x}{y}\right)^m = \frac{x^m}{y^m}$  (Power of a Quotient Property)
- $x^{-m} = \frac{1}{x^m}$  (Negative Exponent Property)

## 6-01 Exponent Properties and e (5.2, 6.2)

- Simplify the expression. Write your answer using only positive exponents.

• Try 292#1

$$\bullet 6b^0$$

- Example 292#3

$$\bullet \left(\frac{3w}{2x}\right)^4$$

$$\left(\frac{3w}{2x}\right)^4 = \frac{3^4 w^4}{2^4 x^4} = \frac{81w^4}{16x^4}$$

$$6b^0 = 6 \cdot 1 = 6$$

## 6-01 Exponent Properties and $e$ (5.2, 6.2)

- $e$ 
  - Called the natural base
  - Named after Leonard Euler who discovered it
    - (Pronounced “oil-er”)
  - Found by putting really big numbers into  $\left(1 + \frac{1}{n}\right)^n = 2.718281828459\dots$
  - Irrational number like  $\pi$

## 6-01 Exponent Properties and $e$ (5.2, 6.2)

- Simplifying natural base expressions
    - Just treat  $e$  like a regular variable
  - Example (305#5)
    - $(5e^{7x})^4$
- Try 305#3
- $\frac{11e^9}{22e^{10}}$

$$(5e^{7x})^4 = 5^4 e^{7x \cdot 4} = 625e^{28x}$$

$$\frac{11e^9}{22e^{10}} = \frac{1}{2} e^{9-10} = \frac{1}{2} e^{-1} = \frac{1}{2e}$$

## 6-01 Exponent Properties and $e$ (5.2, 6.2)

- Evaluate the natural base expressions using your calculator
- Example 305#29
  - Rewrite in the form  $y = ab^x$
  - $y = e^{-0.75t}$
- Try 305#31
  - $y = 2e^{0.4t}$

$$y = e^{-0.75t} = (e^{-0.75})^t = 0.472^t$$

$$y = 2e^{0.4t} = 2(e^{0.4})^t = 2(1.492)^t$$



## 6-01 Exponent Properties and $e$ (5.2, 6.2)

- Assignment (20 total)
  - Properties of Exponents: 292#1-4;
  - Simplifying  $e$ : 305#1-10 odd;
  - Changing  $e$  to decimal: 305#25-28 all;
  - Mixed Review: 306#43, 45, 51, 53 (no graph), 55 (no graph)

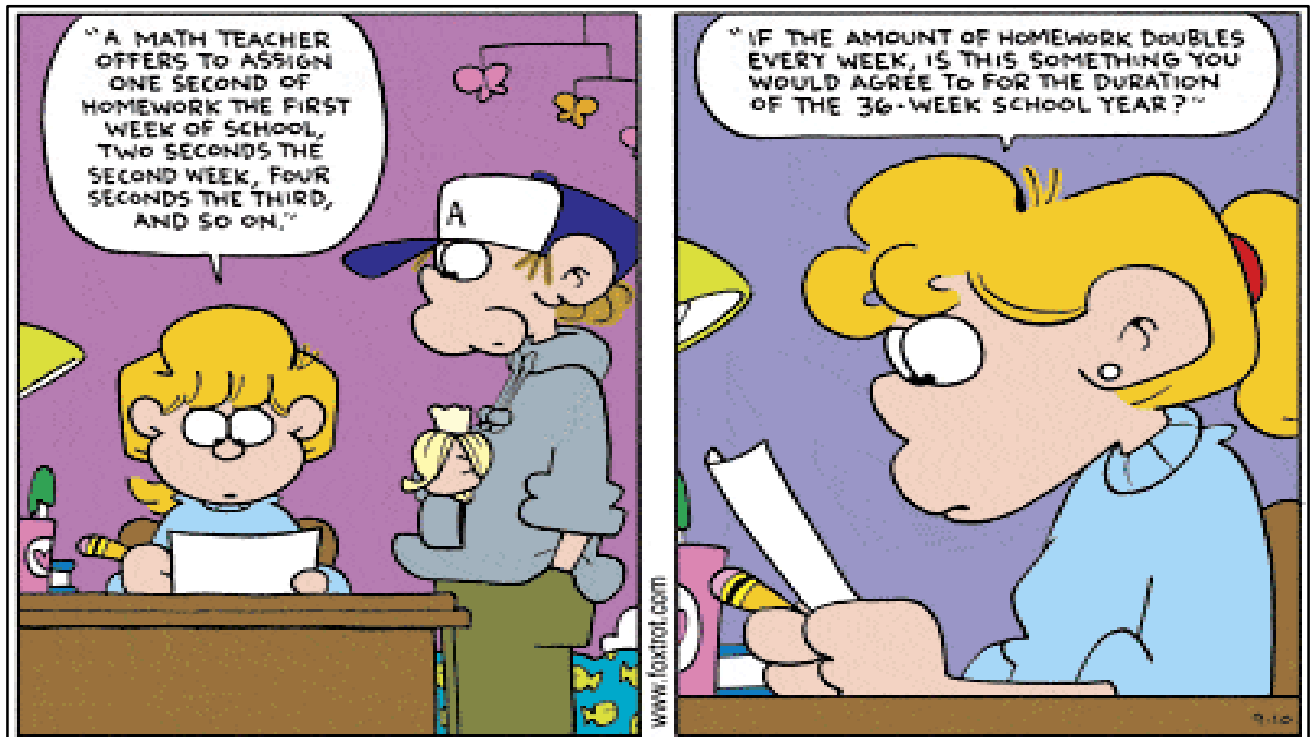
## *6-02 Exponential Growth and Decay Functions (6.1)*

After this lesson...

- I can identify and graph exponential growth and decay functions.
- I can write exponential growth and decay functions.
- I can solve real-life problems using exponential growth and decay functions.

6-02 Exponential Growth and Decay Functions (6.1)





How much work will be done the last week of school?

Formula is  $2^{n-1}$

Plug in 36:  $2^{36-1} = 3.436 \times 10^{10}$  seconds  $\rightarrow$  9544371.769 hours  $\rightarrow$  397682.157 days  $\rightarrow$  1088.8 years



## 6-02 Exponential Growth and Decay Functions (6.1)

### Work with a partner.

Calculate how much time you will spend on your homework the last week of the 36-week school year. You start with 1 second of homework on week one and double the time every week.

$$2^{35}$$

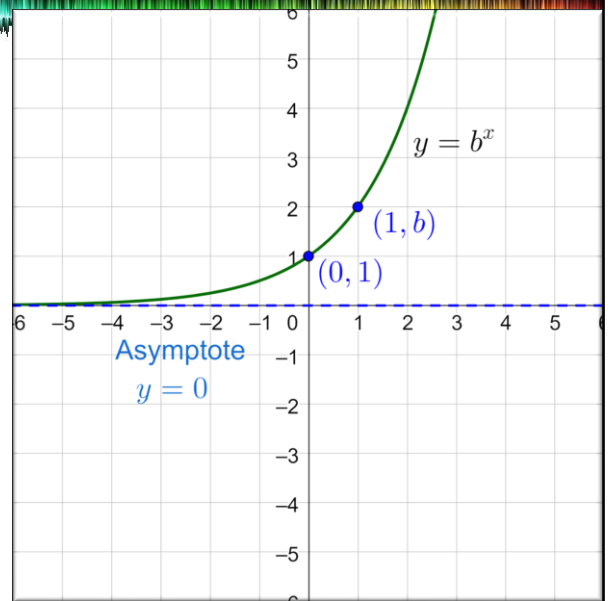
## 6-02 Exponential Growth and Decay Functions (6.1)

### • Exponential Function

- $y = b^x$
- Base ( $b$ ) is a positive number other than 1

### • Exponential Growth

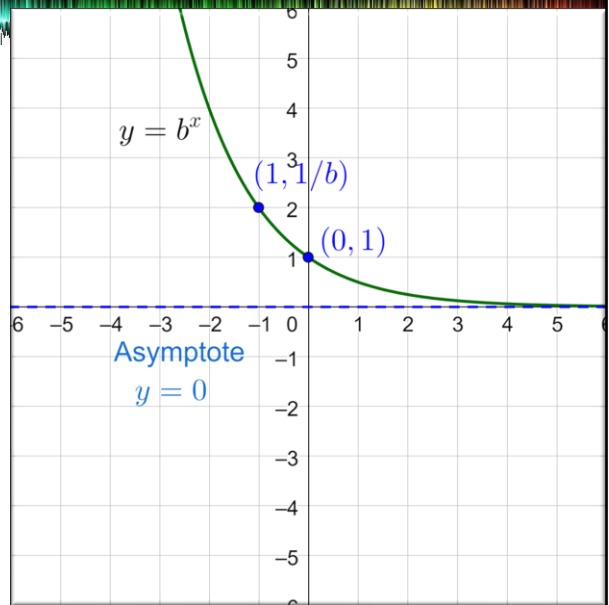
- Always increasing and rate of change is increasing
- $b > 1$
- $y$ -intercept is  $(0, 1)$
- Horizontal asymptote  $y = 0$
- $b$  is the growth factor



## 6-02 Exponential Growth and Decay Functions (6.1)

### • Exponential Decay

- Always decreasing and rate of change is decreasing
- $0 < b < 1$
- $y$ -intercept is  $(0, 1)$
- Horizontal asymptote  $y = 0$
- $b$  is the decay factor

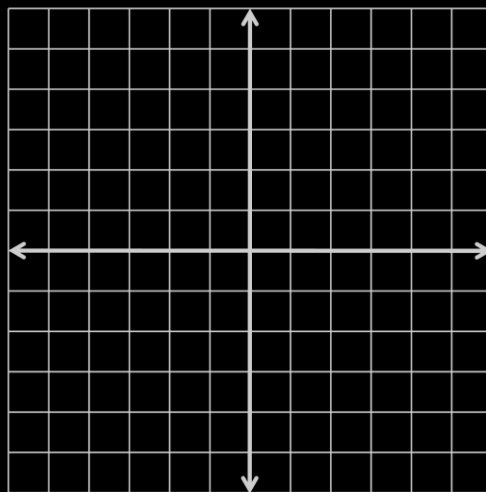




## 6-02 Exponential Growth and Decay Functions (6.1)

- Example 298#9
- Determine whether each function represents *exponential growth* or *exponential decay*. Then graph the function.

$$f(x) = \left(\frac{1}{6}\right)^x$$

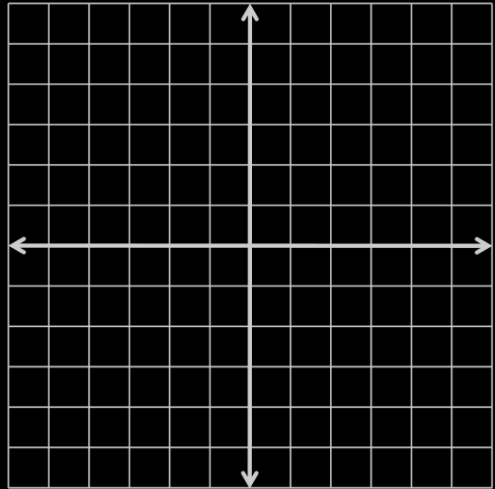


$b = 1/6 < 1$  exponential decay

## 6-02 Exponential Growth and Decay Functions (6.1)

- Try 298#11
- Determine whether each function represents *exponential growth* or *exponential decay*. Then graph the function.

$$y = \left(\frac{4}{3}\right)^x$$



$b = 4/3 > 1$  exponential growth

## 6-02 Exponential Growth and Decay Functions (6.1)

• Exponential Growth Model (word problems)

- $y = a(1 + r)^t$
- $y$  = current amount
- $a$  = initial amount
- $r$  = growth percent
- $1 + r$  = growth factor
- $t$  = time

• Exponential Decay Model (word problems)

- $y = a(1 - r)^t$
- $y$  = current amount
- $a$  = initial amount
- $r$  = decay percent
- $1 - r$  = decay factor
- $t$  = time

## 6-02 Exponential Growth and Decay Functions (6.1)

- Example: 298#20
  - The population  $P$  (in millions) of Peru during a recent decade can be approximated by  $P = 28.22(1.01)^t$ , where  $t$  is the number of years since the beginning of the decade.
  - (a) Determine whether the model represents exponential growth or decay
  - (b) identify the annual percent increase or decrease in population
  - (c) Estimate when the population was about 30 million

a) Base is  $1.01 > 1$  growth

b)  $1.01 = 1 + r \rightarrow 0.01 = r = 1\%$

c)  $30 = 28.22(1.01)^t$

$$1.063 = 1.01^t$$

$$\log_{1.01} 1.063 = \log_{1.01} 1.01^t$$

$$6.15 = t$$

about 6.2 years since the beginning of the decade

## 6-02 Exponential Growth and Decay Functions (6.1)

- Try 298#19
- The value of a mountain bike  $y$  (in dollars) can be approximated by the model  $y = 200(0.65)^t$ , where  $t$  is the number of years since the bike was purchased.
- (a) Determine whether the model represents exponential growth or decay
- (b) Identify the annual percent increase or decrease
- (c) Estimate when the value of the bike will be \$50

a) Base =  $0.65 < 1$  decay

b)  $0.65 = 1 - r \rightarrow -0.35 = -r \rightarrow r = 0.35 = 35\%$

c)  $50 = 200(0.65)^t$

$$0.25 = 0.65^t$$

$$\log_{0.65} 0.25 = \log_{0.65} 0.65^t$$

$$3.22 = t$$

about 3.2 years after it was purchased

## 6-02 Exponential Growth and Decay Functions (6.1)

### • Compound Interest

$$A = P \left( 1 + \frac{r}{n} \right)^{nt}$$

- $A$  = amount at time  $t$
- $P$  = principle (initial amount)
- $r$  = annual rate
- $n$  = number of times interest is compounded per year

• Example: 299#39

- Find the balance in the account earning compound interest after 6 years when the principle is \$3500.  $r = 2.16\%$ , compounded quarterly

• Try 299#41

$$A = P \left( 1 + \frac{r}{n} \right)^{nt}$$
$$A = 3500 \left( 1 + \frac{0.0216}{4} \right)^{4(6)} = \$3982.92$$

$$A = 3500 \left( 1 + \frac{0.0126}{12} \right)^{12(6)} = \$3688.56$$

## 6-02 Exponential Growth and Decay Functions (6.1)

- Assignment: 20 total
  - Graphing Exponential Growth and Decay: 298#7-15 odd
  - Exponential Growth and Decay Models: 298#19-22, 44
  - Compound Interest: 299#35, 39, 40, 41, 42
  - Mixed Review: 300#53, 54, 55, 61, 63

## *6-03 Rewrite Exponential as Logarithmic Functions (6.3)*

After this lesson...

- I can evaluate logarithms.
- I can rewrite exponential equations as logarithmic equations.
- I can rewrite logarithmic equations as exponential equations.



## 6-03 Rewrite Exponential as Logarithmic Functions (6.3)

- Logarithms are exponents
  - $\log_b a =$  exponent of  $b$  to get  $a$
- Example:  $3^{12} = 531441$ 
  - $\log_3 81$
- Try  $3^{12} = 531441$ 
  - $\log_3 3$

Can use trial and error

$$\begin{aligned}\log_3 81 \\ 3^x &= 81 \\ x &= 4\end{aligned}$$

$$\begin{aligned}\log_3 3 \\ 3^x &= 3 \\ x &= 1\end{aligned}$$

## 6-03 Rewrite Exponential as Logarithmic Functions (6.3)

- Calculator has two logs
  - Common Log:  $\log = \log_{10}$
  - Natural Log:  $\ln = \log_e$
- (Some calculators can do log of any base.)
- Example: 312#23
  - $\log 6$
  - Try 312#25
    - $\ln \frac{1}{3}$

$$\log 6 = 0.778$$

$$\ln \frac{1}{3} = -1.099$$

## 6-03 Rewrite Exponential as Logarithmic Functions (6.3)

- Definition of Logarithm with Base  $b$

$$\bullet \log_b y = x \Leftrightarrow b^x = y$$

- Read as “log base  $b$  of  $y$  equals  $x$ ”
- Logs = exponents!!
- Logs and exponentials are inverses
  - They undo each other
  - They cancel each other out

$$3^2 = 9$$

$$8^0 = 1$$

$$5^{-2} = 1/25$$

## 6-03 Rewrite Exponential as Logarithmic Functions (6.3)

- Example: 312#1
  - Rewrite as an exponential
  - $\log_3 9 = 2$
- Try 312#7
  - Rewrite as a log
  - $6^2 = 36$

Base = 3, exponent = 2, other = 9

$$\log_3 9 = 2$$

$$3^2 = 9$$

Base = 6, exponent = 2, other = 36

$$6^2 = 36$$

$$\log_6 36 = 2$$

## 6-03 Rewrite Exponential as Logarithmic Functions (6.3)

- Simplify log expressions

- If exponential with base  $b$  and log with base  $b$  are inside each other, they cancel

- Example: 312#31

- $7^{\log_7 x}$

- Try 312#35

- $\log_3 3^{2x}$

$$7^{\log_7 x} = \cancel{7}^{\log_7 x} = x$$

$$\log_3 3^{2x} = \log_3 \cancel{3}^{2x} = 2x$$

## 6-03 Rewrite Exponential as Logarithmic Functions (6.3)

- Assignment (20 total)
  - Evaluate logs: 312#13, 15, 17, 23, 25
  - Rewrite logs as exponentials: 312#1, 3, 5
  - Rewrite exponentials as logs: 312#7, 9, 11
  - Simplify expressions: 312#31, 33, 35, 37
  - Mixed Review: 314#75, 77, 79, 83, 85

## 6-04 *Logarithmic Properties (6.5)*

After this lesson...

- I can expand logarithms.
- I can condense logarithms.
- I can evaluate logarithms using the change-of-base formula.

## 6-04 Logarithmic Properties (6.5)



- Product Property

- $\log_b uv = \log_b u + \log_b v$

- Quotient Property

- $\log_b \frac{u}{v} = \log_b u - \log_b v$

- Power Property

- $\log_b u^n = n \log_b u$



## 6-04 Logarithmic Properties (6.5)

- Expand logarithms

- Rewrite as several logs

- Example: 327#13

- $\log 10x^5$

- Try 327#15

- $\ln \frac{x}{3y}$

Product property

$$\log 10x^5$$

Power property

$$\log 10 + \log x^5$$

Simplify

$$\log 10 + 5 \log x$$

$$1 + 5 \log x$$

Quotient and power properties

$$\ln \frac{x}{3y}$$

$$\ln x - \ln 3 - \ln y$$

## 6-04 Logarithmic Properties (6.5)

- Condense logs

- Try to write as a single log

- Try 327#23

- $6 \ln x + 4 \ln y$

- Example: 327#25

- $\log_5 4 + \frac{1}{3} \log_5 x$

$$\log_5 4 + \frac{1}{3} \log_5 x$$

Power Property

$$\log_5 4 + \log_5 x^{\frac{1}{3}}$$

Product Property

$$\log_5 \left( 4x^{\frac{1}{3}} \right)$$

Write as radical (because of fractional exponent)

$$\log_5 4 \sqrt[3]{x}$$

$$6 \ln x + 4 \ln y$$

Power Property

$$\ln x^6 + \ln y^4$$

Product property

$$\ln x^6 y^4$$

## 6-04 Logarithmic Properties (6.5)

### • Change-of-Base Formula

$$\bullet \log_c u = \frac{\log_b u}{\log_b c}$$

- This lets you evaluate any log on a calculator

### • Example: 327#31

- Evaluate  $\log_9 15$

### • Try 327#29

- Evaluate  $\log_4 7$

$$\log_9 15 = \frac{\log 15}{\log 9} = 1.232$$

$$\log_4 7 = \frac{\log 7}{\log 4} = 1.404$$

## 6-04 Logarithmic Properties (6.5)

- Assignment: 20 total
  - Expand logs: 327#11-17 odd
  - Condense logs: 327#21-27 odd
  - Change-of-base formula: 327#29-35 odd
  - Problem Solving: 327#37-38 (Use  $L = 10 \log \frac{I}{10^{-12}}$ )
  - Mixed Review: 328#46, 47, 51, 57, 59, 61

## *6-05 Graph Exponential and Logarithmic Functions (6.4)*

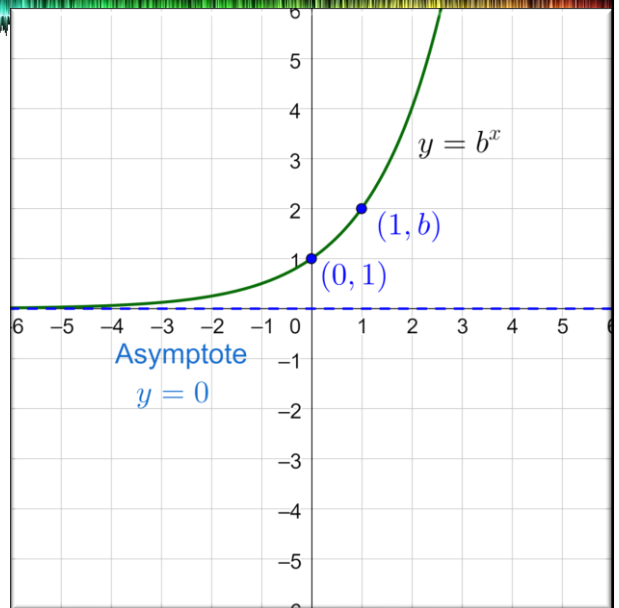
After this lesson...

- I can graph exponential functions.
- I can graph logarithmic functions.
- I can find inverses of exponential and logarithmic functions.

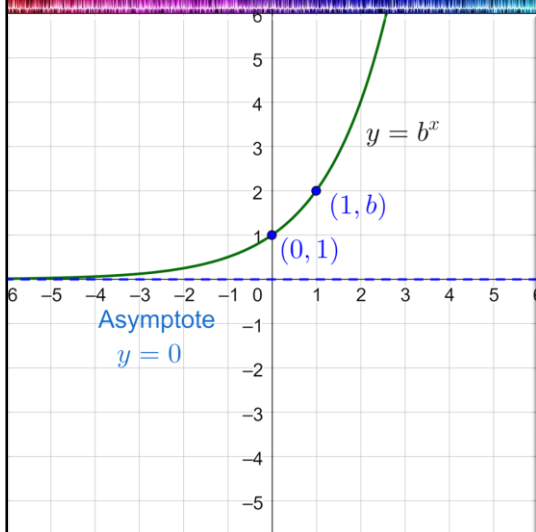
## 6-05 Graph Exponential and Logarithmic Functions (6.4)

### • Exponential Function

- $y = b^x$
- Base ( $b$ ) is a positive number other than 1
- In general
  - $y = ab^{cx-h} + k$
  - $a$  is vertical stretch
    - If  $a$  is  $-$ , reflect over  $x$ -axis
  - $c$  is horizontal shrink
    - Shrink by  $\frac{1}{c}$
    - If  $b$  is  $-$ , reflect over  $y$ -axis
  - $h$  is horizontal shift
  - $k$  is vertical shift
  - Horizontal asymptote:  $y = k$



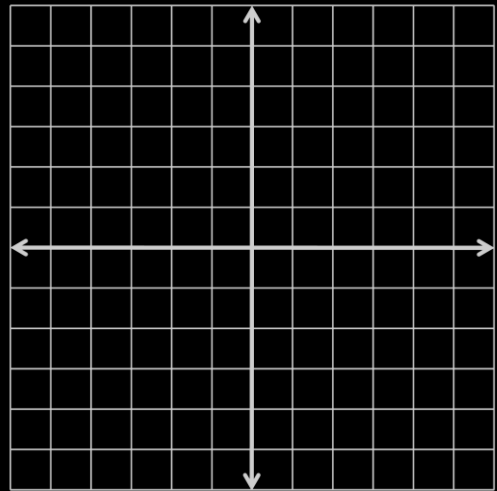
## 6-05 Graph Exponential and Logarithmic Functions (6.4)



- Graph Exponential Functions
  - Find and graph the horizontal asymptote
  - Make a table of values
  - Plot points and draw the curve
    - Make sure the curve is near the asymptotes at the edge of the graph

## 6-05 Graph Exponential and Logarithmic Functions (6.4)

- Example: 320#17
- (a) Describe the transformations. (b) Then graph the function.  
 $g(x) = -2^{x-3}$



Transformations:  $a = -1$ ,  $h = 3$ ,  $k = 0$

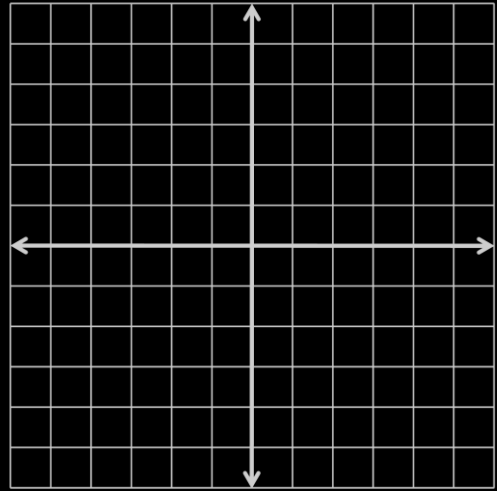
Reflection in  $x$ -axis ( $-a$ ) and shift 3 to right

Horizontal asymptote:  $y = 0$



## 6-05 Graph Exponential and Logarithmic Functions (6.4)

- Try 320#15
- (a) Describe the transformations. (b) Then graph the function.  
 $g(x) = e^{2x}$

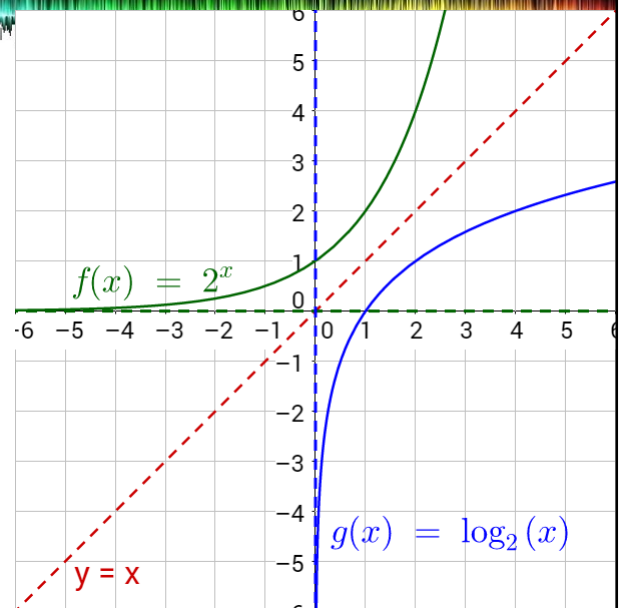


Transformations:  $a = 1, c = 2, h = 0, k = 0$   
Horizontal shrink by factor of  $1/2$   
Horizontal asymptote:  $y = 0$

## 6-05 Graph Exponential and Logarithmic Functions (6.4)

### • Logarithmic Function

- $y = \log_b x$
- Base ( $b$ ) is a positive number other than 1
- Logarithms and exponentials are inverses
- $x$  and  $y$  are switched
- Graphically, reflected over  $y = x$
- Horizontal asymptote becomes vertical asymptote



## 6-05 Graph Exponential and Logarithmic Functions (6.4)

- In general

- $y = a \log_b(cx - h) + k$
- $a$  is vertical stretch
  - If  $a$  is  $-$ , reflect over  $x$ -axis
- $c$  is horizontal shrink
  - Shrink by  $\frac{1}{c}$
  - If  $b$  is  $-$ , reflect over  $y$ -axis
- $h$  is horizontal shift
- $k$  is vertical shift
- Vertical asymptote:  $x = h$

- Graph Logarithmic Functions

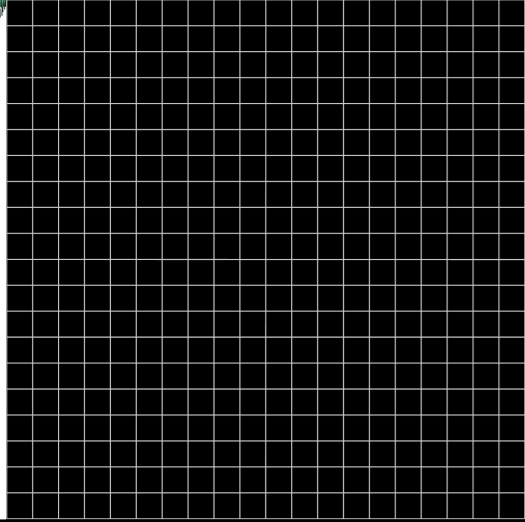
- Find and graph the vertical asymptote
- Make a table of values
  - You may need to use the change-of-base formula
- Plot points and draw the curve
  - Make sure the curve is near the asymptotes at the edge of the graph

*To put in calculator, you might need to use change-of-base formula*

$$y = \log_3 x$$
$$y = \frac{\log x}{\log 3}$$

## 6-05 Graph Exponential and Logarithmic Functions (6.4)

- Example: 320#27
- (a) Describe the transformations. (b) Then graph the function.  
 $g(x) = -\log_{1/5}(x - 7)$



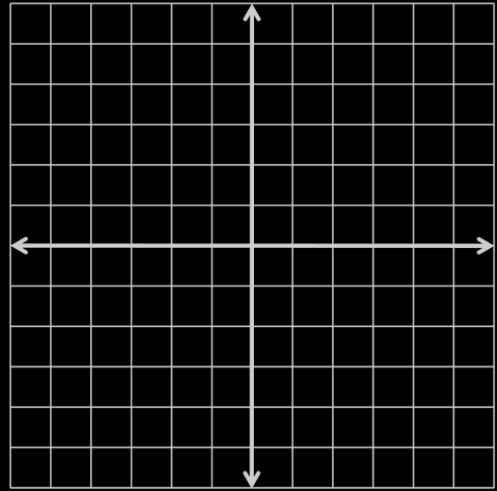
Transformations:  $a = -1$ ,  $h = 7$ ,  $k = 0$

Reflection in  $x$ -axis ( $-a$ ) and shift 7 to right

Vertical asymptote:  $x = 7$

## 6-05 Graph Exponential and Logarithmic Functions (6.4)

- Try 320#25
- (a) Describe the transformations. (a)  
Then graph the function.  
 $g(x) = 3 \log_4 x - 5$



Transformations:  $a = 3$ ,  $h = 0$ ,  $k = -5$   
Vertical stretch by factor of 3; vertical shift up 5  
Vertical asymptote:  $x = 0$

## 6-05 Graph Exponential and Logarithmic Functions (6.4)

### • Find the inverse

- Isolate log or exponential part
- Switch  $x$  and  $y$
- Then rewrite as exponential or log

### • Example: 313#47

- $y = \ln(x - 1)$

### • Try 313#51

- $y = 5^x - 9$

$$y = \ln(x - 1)$$

$$x = \ln(y - 1)$$

Base =  $e$ , exponent =  $x$ , other =  $y - 1$

$$y - 1 = e^x$$

$$y = e^x + 1$$

$$y = 5^x - 9$$

$$y - 9 = 5^x$$

$$x - 9 = 5^y$$

Base =  $5$ , exponent =  $y$ , other  $x - 9$

$$y = \log_5(x - 9)$$

## 6-05 Graph Exponential and Logarithmic Functions (6.4)

- Assignment: 15 total
  - Graph Exponential Functions: 320#15, 17, 21
  - Graph Logarithmic Functions: 313#57, 59; 320#25, 27
  - Find Inverses: 313#43, 45, 47, 51
  - Mixed Review: 322# 53, 55, 62, 65

## *6-06 Solve Exponential and Logarithmic Equations (6.6)*

After this lesson...

- I can solve exponential equations.
- I can solve logarithmic equations.



## 6-06 Solve Exponential and Logarithmic Equations (6.6)

### • Solving Exponential Equations

- Method 1) if the bases are equal, then exponents are equal

### • Example: 334#3

- $5^{x-3} = 25^{x-5}$

### • Try 334#1

- $2^{3x+5} = 2^{1-x}$

$$5^{x-3} = 25^{x-5}$$

Write at same base

$$5^{x-3} = 5^{2(x-5)}$$

Since bases are same, exponents are the same

$$x - 3 = 2(x - 5)$$

$$x - 3 = 2x - 10$$

$$-3 = x - 10$$

$$7 = x$$

$$2^{3x+5} = 2^{1-x}$$

Since bases are same, exponents are the same

$$3x + 5 = 1 - x$$

$$4x + 5 = 1$$

$$4x = -4$$

$$x = -1$$

## 6-06 Solve Exponential and Logarithmic Equations (6.6)

### • Solving Exponential Equations

- Method 2) take log of both sides

### • Example: 334#9

- $5(7)^{5x} = 60$

### • Try 334#11

- $3e^{4x} + 9 = 15$

$$5(7)^{5x} = 60$$
$$7^{5x} = 12$$

Log both side with base 7

$$\log_7 7^{5x} = \log_7 12$$
$$5x = \log_7 12$$
$$x = \frac{\log_7 12}{5} \approx 0.255$$

$$3e^{4x} + 9 = 15$$
$$3e^{4x} = 6$$
$$e^{4x} = 2$$

Log both sides with base e

$$\ln e^{4x} = \ln 2$$
$$4x = \ln 2$$
$$x = \frac{\ln 2}{4} \approx 0.173$$

## 6-06 Solve Exponential and Logarithmic Equations (6.6)

### • Solving Logarithmic Equations

- Method 1) if the bases are equal, then logs are equal

### • Example 334#17

- $\ln(4x - 12) = \ln x$

### • Try 334#19

- $\log_2(3x - 4) = \log_2 5$

$$\ln(4x - 12) = \ln x$$

Since logs are the same, the stuff in logs are the same

$$4x - 12 = x$$

$$-12 = -3x$$

$$4 = x$$

$$\log_2(3x - 4) = \log_2 5$$

Since logs are the same, the stuff in the logs are the same

$$3x - 4 = 5$$

$$3x = 9$$

$$x = 3$$

## 6-06 Solve Exponential and Logarithmic Equations (6.6)

### • Solving Logarithmic Equations

- Method 2) exponentiating both sides

- Make both sides exponents with the base of the log

- Example: 334#21

- $\log_2(4x + 8) = 5$

- Try 334#22

- $\log_3(2x + 1) = 2$

Exponentiate with base 2

$$\log_2(4x + 8) = 5$$

$$2^{\log_2(4x+8)} = 2^5$$

$$4x + 8 = 32$$

$$4x = 24$$

$$x = 6$$

Exponentiate with base 3

$$\log_3(2x + 1) = 2$$

$$3^{\log_3(2x+1)} = 3^2$$

$$2x + 1 = 9$$

$$2x = 8$$

$$x = 4$$

## 6-06 Solve Exponential and Logarithmic Equations (6.6)

- Assignment (20 total)
  - Solve Exponential Equations: 334#1, 3, 5, 7, 9, 11, 13
  - Solve Logarithmic Equations: 334#17, 19, 21, 22, 23, 25, 27, 29
  - Mixed Review: 336#75, 77, 79, 83, 87

## *6-07 Modeling with Exponential and Logarithmic Functions (6.7)*

After this lesson...

- I can use a common ratio to determine whether data can be represented by an exponential function.
- I can use technology to find exponential models and logarithmic models for sets of data.

## 6-07 Modeling with Exponential and Logarithmic Functions (6.7)

- Choosing Functions to Model Data
- For equally spaced x-values
  - If y-values have common ratio (multiple) → exponential
  - If y-values have finite differences → polynomial

## 6-07 Modeling with Exponential and Logarithmic Functions (6.7)

- Determine the type of function represented by each table.
- Try 342#1

- Example: 342#3

x	5	10	15	20	25	30
y	4	3	7	16	30	49

x	0	3	6	9	12	15
y	0.25	1	4	16	64	256

Finite differences

4 3 7 16 30 49  
 -1 4 9 14 19  
 5 5 5 5

2<sup>rd</sup> order differences are constant → quadratic

Common ratio  $r = 4$  → exponential



## 6-07 Modeling with Exponential and Logarithmic Functions (6.7)

- Use the regression feature on a graphing calculator
  - TI-84
  - Enter points in STAT → EDIT
    - To see points go Y= and highlight Plot1 and press ENTER to keep it highlighted
    - Press Zoom and choose ZoomStat
  - Go to STAT → CALC → ExpReg for exponential OR LnReg for logarithmic
- NumWorks
  - Choose Regression from homescreen
  - In Data tab, enter points
  - Go to Graph tab
    - To change regression type, press OK and choose a different regression
    - Read the answer off the bottom of the graph

## 6-07 Modeling with Exponential and Logarithmic Functions (6.7)

- Determine whether the data show an exponential relationship. Then write a function that models the data.

- Try 342#19

x	1	6	11	16	21
y	12	28	76	190	450

- Example 342#20

x	-3	-1	1	3	5
y	2	7	24	68	194

Use technology

$$y = 11.12(1.77)^x$$

$$y = 8.88(1.21)^x$$

## 6-07 Modeling with Exponential and Logarithmic Functions (6.7)

- Assignment: 15 total
  - Determine Type of Model: 342#1-4
  - Find Model from Table: 342#19, 20, 21, 22, 30, 31, 32
  - Mixed Review: 344#39, 41, 47, 49